

CONSTRAINTS →

The limitations on the motion of the system are called constraints. A constrained motion is a motion which can not proceed arbitrarily in any manner.

Type of constraints

(1) Holonomic constraints →

constraints can be expressed in the form of equations connecting the co-ordinates of the particles at time 't' then the constraints are called holonomic constraints.

$$\text{i.e. } F(x_1, x_2, \dots, x_N, t) = 0$$

Ex →

The motion of the bob of a simple pendulum.

(2) Non-holonomic constraints →

constraints can not be expressed in the form of equation (dependent of velocity)

$$f(x_1, x_2, \dots, t) \leq 0$$

May involve in equalities

May involve non integrable differential equation

$$\text{Ex - } \frac{d\theta}{dt} = \text{constant}$$

(not can expressed in equation form)

(i). Motion of a particle on the surface of sphere which radius (a)

$$\text{then } |r| \geq a$$

$$\boxed{r - a \geq 0}$$

— + —